On the Robustness of Next Generation GNSS Phase-only Real-Time Kinematic Positioning

Lennard HUISMAN\(^1\), Peter J.G. TEUNISSEN\(^1,2\), Dennis ODIJK\(^1\)

\(^1\)Curtin University of Technology
GNSS Research Lab
Kent Street, Bentley
WA 6845, Perth, Australia

\(^2\)Delft University of Technology
DEOS-MGP
Kluyverweg 1
2629 HS, Delft, The Netherlands

**Key words:** Phase-only RTK, GNSS, multipath

**SUMMARY**

The coming years will show a proliferation of Global and Regional Navigation Satellite Systems (GNSS). This promise of a broader multi-frequency, multi-constellation "system of systems" has the potential to enable a wide range of demanding applications for high-accuracy users. For such applications, successful GNSS ambiguity resolution, which is the process of resolving the unknown cycle ambiguities of double-difference (DD) carrier-phase data as integers, is essential. The sole purpose of ambiguity resolution is to use the integer ambiguity constraints as a means of improving significantly on the precision of the remaining model parameters, such as baseline coordinates and/or atmospheric delays. Ambiguity resolution applies to a great variety of current and future GNSS models. These models differ greatly in complexity and diversity. They range from single-baseline models used for real-time kinematic (RTK) positioning to multi-baseline models used as a tool for studying geodynamic phenomena. The increase in signals, frequencies and satellites has enormous potential for increasing the robustness of GNSS models.

In this contribution we study and analyze the robustness of multi-frequency GNSS models for phase-only RTK processing. Our attention is restricted to the short baseline application, neglecting the influence of atmospheric errors, but it is stressed that the phase-only RTK model is also applicable for longer baselines. We use the ambiguity success-rate as our measure for phase only performance. Using experimental results we show that the phase-only RTK model is more robust in case of multipath than the traditional phase+code RTK model.
1. INTRODUCTION

Global Navigation Satellite System (GNSS) ambiguity resolution is the process of resolving the unknown cycle ambiguities of double difference (DD) carrier phase data as integers. The sole purpose of ambiguity resolution is to use the integer ambiguity constraints as a means of improving significantly on the precision of the remaining model parameters, such as baseline coordinates and/or atmospheric delays.

Ambiguity resolution applies to a great variety of current and future GNSS models. These models may differ greatly in complexity and diversity. They range from single-baseline models used for kinematic positioning to multi-baseline models used as a tool for studying geodynamic phenomena. The models may or may not have the relative receiver-satellite geometry included. They may also be discriminated as to whether the slave receiver(s) are stationary or in motion. When in motion, one solves for one or more trajectories, since with the receiver-satellite geometry included, one will have new coordinate unknowns for each epoch. One may also discriminate between the models as to whether or not the differential atmospheric delays are included as unknowns. In the case of sufficiently short baselines they are usually excluded. Apart from the current Global Positioning System (GPS) models, carrier phase ambiguity resolution also applies to the future modernized GPS and the future European Galileo GNSS. An overview of GNSS models, together with their applications in surveying, navigation, geodesy and geophysics, can be found in textbooks such as [Parkinson and Spilker, 1996], [Strang and Borre, 1997], [Teunissen and Kleusberg, 1998], [Leick, 2004], [Misra and Enge, 2006], [Hofmann-Wellenhof et al., 2008].

In this contribution we study and analyze the robustness of current and modernized GPS models for phase-only RTK processing (see table 1). The methodology developed is generally applicable and can therefore also be applied to other GNSSs. Short baselines without atmospheric delays are considered. The phase-only GPS model for short-baselines is full of rank providing a minimum of two epochs are used.

<table>
<thead>
<tr>
<th>carrier signal</th>
<th>notation</th>
<th>frequency (MHz)</th>
<th>wave length (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$L_1$</td>
<td>$\phi_1$</td>
<td>$154 \times 10.23 = 1575.420$</td>
<td>$\lambda_1 = 19.03$</td>
</tr>
<tr>
<td>$L_2$</td>
<td>$\phi_2$</td>
<td>$120 \times 10.23 = 1227.600$</td>
<td>$\lambda_2 = 24.42$</td>
</tr>
<tr>
<td>$L_5$</td>
<td>$\phi_3$</td>
<td>$115 \times 10.23 = 1176.450$</td>
<td>$\lambda_3 = 25.48$</td>
</tr>
</tbody>
</table>

Table 1: Modernized GPS signals

We study the impact of the third GPS frequency, the number of satellites and the measurement precision on phase-only processing. We use the ambiguity success-rate as our
measure for phase only performance. The potential advantage of using carrier phase-only data is that ambiguity resolution will be freed from any biasing effects that the code data may bring (e.g. code multipath). Using experimental results we show that the phase-only RTK model is more robust in case of multipath than the traditional phase+code RTK model.

2. INTEGER AMBIGUITY RESOLUTION

2.1 The GNSS model

In principle all GNSS models can be cast in the following frame of linear(ized) observation equations,

\[ E(y) = Aa + Bb, \quad D(y) = Q_y \], \quad a \in Z^n, \quad b \in R^p \quad (1)\]

where \( y \) is the given GNSS data vector of order \( m \), \( a \) and \( b \) are the unknown parameter vectors respectively of order \( n \) and \( p \), \( E \) and \( D \) are the expectation and dispersion operator, respectively, \( A \) and \( B \) are the given design matrices that link \( y \) to \( a \) and \( b \), and where \( Q_y \) is the given variance matrix of \( y \). The data vector \( y \) may consist of the 'observed minus computed' single-, dual- or triple frequency double-difference (DD) phase and/or pseudorange (code) observations accumulated over all observation epochs. The entries of vector \( a \) are then the DD carrier phase ambiguities, expressed in units of cycles rather than range. They are known to be integers, \( a \in Z^n \). The entries of the vector \( b \) will consist of the remaining unknown parameters, such as for instance baseline components (coordinates) and possibly atmospheric delay parameters. They are known to be real-valued, \( b \in R^p \).

When using the least-squares (LS) principle, the GNSS model can be solved by means of the minimization problem

\[ \min_{a,b} \| y - A\hat{a} - B\hat{b} \|_{Q_y}^2, \quad a \in Z^n, \quad b \in R^p \quad (2) \]

with \( \| \cdot \|_{Q_y}^2 = (\cdot)^T Q_y^{-1} (\cdot) \).

The solution of this integer LS problem can be obtained in the following three steps,

\[
\left\{
\begin{array}{l}
(i) \quad \hat{a}, \hat{b} = \arg\min_{a,b} \| y - Aa - Bb \|_{Q_y}^2 \\
(ii) \quad \tilde{a} = \arg\min_{a \in Z^n} \| \hat{a} - a \|_{Q_y}^2 \\
(iii) \quad \tilde{b} = \hat{b} - Q_{ha}^{-1} \tilde{a} (\hat{a} - \tilde{a})
\end{array}
\right. \quad (3)
\]

In the first step one simply discards the integer constraints \( a \in Z^n \) on the ambiguities and performs a standard LS adjustment. As a result one obtains the (real-valued) LS estimates \( \hat{a} \) and \( \hat{b} \), together with their variance matrix. The solution of this first step is referred to as the 'float' solution. In the second step the 'float' ambiguity estimate \( \hat{a} \) is used to compute the corresponding integer LS ambiguity estimate \( \tilde{a} \). Once these integer ambiguities are computed, they are used in the third step to finally correct the 'float' estimate of \( \hat{b} \), so as to obtain the 'fixed' estimate \( \tilde{b} \).
The above integer LS solution can be computed efficiently with the popular LAMBDA (Least-squares AMBiguity Decorrelation Adjustment) method, see e.g. [Teunissen, 1995], [de Jonge and Tiberius, 1996].

2.2 The ambiguity success-rate
In order to evaluate the expected performance of ambiguity resolution, we need the probability mass function (PMF) of the estimated ambiguities \( \hat{a} \). If we denote the probability density function (PDF) of \( \hat{a} \) as \( p_\hat{a}(x) \), the PMF of \( \hat{a} \) follows as

\[
P(\hat{a} = z) = \int_{S_z} p_\hat{a}(x) dx, \quad z \in Z^n
\]

with the regions of integration given as \( S_z = \{ x \in \mathbb{R}^n \mid \| x - z \|^2_{Q_{nn}} \leq \| x - u \|^2_{Q_{uu}}, \forall u \in \mathbb{Z}^n \} \) and the PDF - in case of Gaussian distributed data - given as

\[
p_\hat{a}(x) = \frac{1}{\sqrt{\det(Q_{nn})(2\pi)^n}} \exp\left\{-\frac{1}{2}\| x - a \|^2_{Q_{nn}} \right\}
\]

The probability of correct integer ambiguity estimation, \( P(\hat{a} = a) \), is of particular interest. It describes the expected success-rate of GNSS ambiguity resolution. Different ways of evaluating the least-squares success-rate have been given in [Teunissen, 1998]. In the present contribution we make use of the very easy-to-compute lower bound

\[
P(\hat{a} = a) \geq \prod_{i=1}^n \left( 2\Phi\left(\frac{1}{2\sigma_{i,j}}\right) - 1 \right)
\]

with

\[
\Phi(x) = \int_{-\infty}^{x} \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{1}{2}v^2\right\} dv
\]

and where the \( \sigma_{i,j} \), \( i=1,\ldots,n \), denote the sequential conditional standard deviations of the decorrelated ambiguities. This lower bound was introduced in [Teunissen, 1999] and it is presently the sharpest lower bound available for (6), see e.g. [Thomson, 2000], [Verhagen, 2003].

3. SHORT BASELINE PHASE-ONLY AMBIGUITY RESOLUTION

3.1 The short baseline phase-only GPS model
In this section we present the expected performance of phase-only ambiguity resolution for short baselines, using different measurement scenarios. In case of sufficiently short baselines, the unknown ionospheric and tropospheric delays may be assumed absent. The short-baseline, phase+code, multiple frequency model reads,

\[
p_j(i) = G(i)b \\
\phi_j(i) = \lambda_j a_j + G(i)b
\]

with \( p_j(i) \) and \( \phi_j(i), (j=1,2,3) \), respectively the vector of DD code observations and the vector of DD carrier phase data on frequency \( f_j \). \( a_j \) denotes the unknown time invariant
vector of the integer ambiguities of frequency $f_j$ and $b$ the vector of unknown stationary baseline components. The matrix $G(i)$ captures the relative receiver-satellite geometry at epoch $i$, $\lambda_j$ for $j=1,2,3$ denote the known wavelengths of GPS.

The phase-only model lacks the code observations $p_j(i)$:

$$\phi_j(i) = \lambda_j a_j + G(i)b$$

The model is of full-rank from the outset, provided at least two epochs of data are used. Hence, no special precautions have to be taken to eliminate rank defects.

For the standard deviation of observations used in our computations we use an elevation dependent weighting model, which reads,

$$\sigma_{\phi}^2 = \sigma_{\phi}^2 (1 + 10 \exp\{-\frac{\epsilon_s}{10}\})$$

where the elevation dependency is described by the ratio $\frac{\sigma_{\phi}^2}{\sigma_{\phi_i}^2}$ and $\epsilon_s$ the elevation of satellite $s$ in degrees.

### 3.2 Short baseline phase-only success-rates

In the following sections we will look at the dependency of the phase-only GPS-model on the number of frequencies, the number of satellites, the measurement precision and the time interval between measurement epochs. The ambiguity success-rate will be our measure for the performance of the phase-only GPS-model in different scenarios. The ambiguity success-rate will be computed using the lower-bound given in (6). From (6) it is clear that the success-rates depend on the variance-covariance matrix of the decorrelated ambiguities. For a known position and satellite constellation we can perform design computations, without observations, to obtain the expected variance covariance matrix of the decorrelated ambiguities, therefore the expected lower bound for the ambiguity success-rates can be computed without observations.

In the design computations it is assumed that the phase ambiguities remain constant during the complete time span, in this case we can take full advantage of the changing satellite-
receiver geometry. The computations have been performed for a location in Perth, Western Australia, for a dual-epoch observation. The chosen start time for the computations is the first epoch of the experimental data set used in section 3.3. Figure 1 shows a skyplot of the visible satellites above 10 degrees elevation during the time span with this constellation.

3.2.1 Single frequency, Dual frequency and Triple frequency

In this section the influence of the number of satellites and the number of frequencies on the success-rates is investigated. The constellation in figure 1 shows 8 satellites, for the computations with less satellites each time the satellite at the lowest elevation has been removed, so for example in the computations with 6 satellites, satellites with PRN 23 and 31 were removed from the design scenario. Table 2 shows the success-rates for the different scenarios.

<table>
<thead>
<tr>
<th>Frequencies</th>
<th>Success-rate 4 satellites</th>
<th>Success-rate 5 satellites</th>
<th>Success-rate 6 satellites</th>
<th>Success-rate 7 satellites</th>
<th>Success-rate 8 satellites</th>
</tr>
</thead>
<tbody>
<tr>
<td>L1</td>
<td>0.0000</td>
<td>0.0000</td>
<td>0.0002</td>
<td>0.0036</td>
<td>0.1602</td>
</tr>
<tr>
<td>L1/L2</td>
<td>0.2159</td>
<td>0.7564</td>
<td>0.9933</td>
<td>1.0000</td>
<td>1.0000</td>
</tr>
<tr>
<td>L1/L5</td>
<td>0.2500</td>
<td>0.8382</td>
<td>0.9999</td>
<td>1.0000</td>
<td>1.0000</td>
</tr>
<tr>
<td>L2/L5</td>
<td>0.1554</td>
<td>0.9227</td>
<td>1.0000</td>
<td>1.0000</td>
<td>1.0000</td>
</tr>
<tr>
<td>L1/L2/L5</td>
<td>0.9850</td>
<td>1.0000</td>
<td>1.0000</td>
<td>1.0000</td>
<td>1.0000</td>
</tr>
</tbody>
</table>

*Table 2: The phase-only dual-epoch success-rate for different frequencies with 1 second time interval and $\sigma_\phi = 1$ mm*

The table shows that, as can be expected, the more satellites and the more frequencies used the better the success-rates. From the first row it is clear that single-frequency phase-only successful ambiguity resolution is unlikely for short time spans. The success-rate of dual-frequency and triple-frequency are close to one from 6 satellites tracked. The L1/L5 linear combination, which is interesting from a GPS/Galileo combined perspective as Galileo will also broadcast signals on these frequencies, is always outperforming the L1/L2 dual frequency scenario for this constellation.

3.2.2 Measurement precision

The measurement precision has an influence on the success-rates, because it directly influences the precision of the estimated float ambiguities. The value chosen for the coefficient $\sigma_\phi$ in the elevation dependent weighting model of (9) in the previous section is 1 millimeter for all phase observations. The influence of this coefficient on the a-priori standard deviation of the observables versus elevation is shown in figure 2 and the influence on the success-rates is shown in table 3.

<table>
<thead>
<tr>
<th>$\sigma_\phi$ [mm]</th>
<th>Success-rate with 6 satellites</th>
<th>Success-rate with 7 satellites</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.993</td>
<td>1.0000</td>
</tr>
<tr>
<td>2</td>
<td>0.9576</td>
<td>0.9649</td>
</tr>
<tr>
<td>3</td>
<td>0.1878</td>
<td>0.3940</td>
</tr>
</tbody>
</table>

*Table 3: The phase-only dual-epoch success-rate for different measurement precision dual-frequency (L1/L2) observations with 1 second time interval*
The influence of the measurement precision is evident from table 3. It shows the sensitivity of the design computations for not only the number of satellites but also the chosen measurement precision. The measurement precision of currently available GPS-RTK equipment is close to or better than 1 millimeter. For example, the Sokkia equipment used in the experiment in section 3.3 has a specified measurement precision of 0.5 mm for $L1$ and 1 mm for $L2$. A value for the standard deviation of 1 mm in zenith direction when an elevation dependent weighting model is used is also recommended in scientific software such as the Bernese GPS software [Dach et al., 2007]. The results show that dual-epoch phase-only ambiguity resolution should therefore be possible with current surveying grade receivers and 7 satellites in view.

### 3.2.3 Time interval

Although with 6 or more satellites and a state of the art measurement precision the dual-frequency, dual-epoch phase-only success-rates are close to one for a time interval of 1 second, a larger time interval means that the satellite-receiver geometry has changed more, which will make the phase-only model stronger. Figure 3 shows the influence of larger time spans for the single frequency success-rates. The figure shows two lines, one line where all available data, with a time span of 1 second, is used and one line where the first and last epoch, so only two epochs, of the time interval are used for the computation of the success-rates. It is clear from figure 3 that it is not only the redundancy that makes single frequency phase-only ambiguity resolution possible, but also the change in geometry has a strong effect in improving the success-rates. We are only investigating (modernized) GPS at the moment, but it can be expected that more satellite systems will also have a large impact on the single frequency phase-only ambiguity resolution as this will have an impact on both the geometry and the redundancy.

### 3.3 Phase-only fixed baselines in case of multipath

In the previous section we have shown that dual-epoch phase-only ambiguity resolution is possible. In this section we will show the effect of multipath on dual epoch ambiguity resolution and the baseline coordinates in the phase-only and the traditional phase and code
GPS-model. The data used in this section is that of a 100 meter baseline and was collected using Sokkia GSR2700ISX receivers. Figure 4 shows the satellite constellation for the selected measurement interval of 2000 seconds.

Compared to the scenario of the design computations in section 3.2 there is one satellite less (PRN14), which gives 7 satellites that were continuously tracked by both receivers.

### 3.3.1 Multipath simulation

Since the data was collected in a multipath free environment multipath has to be simulated on the observables. In the following sections it is assumed that there is a vertical reflecting surface present that reflects the satellite signals. Figure 5 gives a geometric interpretation of a vertical reflecting surface.
Figure 5: The length of the direct path and the delayed in case of a vertical reflector

There is a direct signal $SR$ from satellite $S$ to receiver $R$ and a reflected signal $SP-PR$, where $P$ is the point of incidence. The length of the reflected path can easily be computed as $SR$ where $S'$ is the image of $S$ in the coordinate system with its origin in the lower left corner of the plane.

The model used for the multipath simulation takes both code and phase multipath into account. The code multipath simulation assumes so-called narrow-sampling and no fractional phase shift as described in [Byun et al., 2002], [Leick, 2004], [Joosten and Irsigler, 2003]. The following expressions are used for the multipath simulations of the code multipath error $\Delta \tau_c$ and the phase multipath error $\Delta \tau_\phi$:

$$\Delta \tau_c(i) = \begin{cases} \frac{\Delta \tau(i) \alpha \cos(\theta(i))}{1 + \Delta \tau(i) \alpha \cos(\theta(i))} & \text{if } \Delta \tau(i) < T_c - I + \Delta \tau_c(i) \\ I \alpha \cos(\theta(i)) & \text{if } T - I + \Delta \tau_c(i) < \Delta \tau(i) < I + \Delta \tau_c(i) \\ \frac{(T_c + I - \Delta \tau(i)) \alpha \cos(\theta(i))}{2 - \Delta \tau(i) \alpha \cos(\theta(i))} & \text{if } I + \Delta \tau_c(i) < \Delta \tau(i) < T_c + I + \Delta \tau_c(i) \\ 0 & \text{if } \Delta \tau(i) > T_c + I + \Delta \tau_c(i) \end{cases}$$

(10)

$$\Delta \tau_\phi(i) = \arctan\left(\frac{\alpha A(i) \sin(\theta(i))}{1 + \alpha A(i) \cos(\theta(i))}\right)$$
with $\alpha$ the attenuation of the reflected signal path, $\theta(i)$ the multipath phase shift at epoch $i$, $T_c$ the chip length of the code signal in seconds, $I$ the sampling interval of the correlator, $\tau(i)$ the time delay of the reflected signal, and $A(i)$ the code correlation function. The code correlation function is sufficiently approximated [Parkinson and Spilker, 1996] by:

$$A(i) = 1 - \frac{\Delta \tau(i)}{T_c}$$  \hspace{1cm} (11)

The multipath phase shift $\theta(i)$ is obtained as follows:

$$\theta(i) = \frac{2\pi}{\lambda} PD(i) = 2\pi f_{c} \Delta \tau(i)$$  \hspace{1cm} (12)

With $PD(i)$ the path delay that can be obtained, see figure 5, by:

$$PD = S'R - SR$$  \hspace{1cm} (13)

### 3.3.2 Multipath scenario

In the simulations for our measurement scenario we have assumed a vertical reflector at an azimuth of $1.45\pi$ with was placed at respectively a distance $d$ of 1 meter, 30 meter and 50 meter. Three values for the attenuation were simulated from very strong reflection ($\alpha=0.9$), to moderate ($\alpha=0.5$) to weak reflections ($\alpha=0.1$), Byun et al. [2002] and Leick [2004] used $\alpha=0.1$ in their contributions. For the $C/A$ code a chip length of 977 ns was used, with a sampling interval of 49 ns. The $P2$ code chip length was set at 98 ns and a sampling interval has been chosen of 65 ns. Figure 6 show the length of the delayed path for the two satellites and the different distances of the reflecting surface to the receiver.

For PRN3 the length of the delayed path increases slowly during the experiment. The delayed path of PRN31 is varying less for the duration of the experiment, but is larger than the delayed path of PRN3. The resulting influence of the multipath on the code and phase observations is shown in figure 7 for the $L1$ frequency and for the $L2$ frequency in figure 8.

![Figure 6: Length of the delayed path for PRN3 (red) and PRN31 (black) for different distance d of the reflecting vertical plane](image-url)
Figure 7: C/A-code (top) and L1-phase (bottom) multipath error for PRN3 (red) and PRN31 (black) in the simulated scenarios.
Figure 8: P2-code (top) and L2-phase (bottom) multipath error for PRN3 (red) and PRN31 (black) in the simulated scenarios
The effect of multipath on the $P2$ code observations is smaller than the code multipath error on the $C\backslash A$ code observations. The $L1$ and $L2$ errors are of the same magnitude.

### 3.3.3 Experimental results

Table 4 shows the empirical success-rates for dual-epoch processing for phase-only ($L1/L2$) observables and phase+code observables ($C\backslash A/L1/P2/L2$). The empirical success-rates without multipath are 0.9980 for phase-only and 1.0000 for phase+code.

<table>
<thead>
<tr>
<th>$\alpha$</th>
<th>$d[m]$</th>
<th>observables</th>
<th>observables</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>$L1/L2$</td>
<td>$C\backslash A/L1/P2/L2$</td>
</tr>
<tr>
<td>0.1</td>
<td>1</td>
<td>0.998</td>
<td>0.885</td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>0.998</td>
<td>0.524</td>
</tr>
<tr>
<td>0.5</td>
<td>1</td>
<td>0.683</td>
<td>0.489</td>
</tr>
<tr>
<td></td>
<td>30</td>
<td>0.811</td>
<td>0.552</td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>0.846</td>
<td>0.528</td>
</tr>
<tr>
<td>0.9</td>
<td>1</td>
<td>0.250</td>
<td>0.472</td>
</tr>
<tr>
<td></td>
<td>30</td>
<td>0.422</td>
<td>0.518</td>
</tr>
<tr>
<td></td>
<td>50</td>
<td>0.530</td>
<td>0.500</td>
</tr>
</tbody>
</table>

*Table 4: The empirical phase-only dual-epoch success-rate*

The table clearly shows the degradation of the empirical success-rates in the presence of code multipath. Even without hardly any code multipath in the case of a distance of the vertical plane of 1 meter and $\alpha=0.1$ (see figures 7 and 8 for the size of the corresponding multipath errors) the success-rate of the code+phase solutions are lower than that of the phase-only processing. With low reflection values ($\alpha=0.1$) the ambiguity resolution of the phase-only processing is almost insensitive for the multipath errors, where the performances of phase-only and code+phase are comparable in strong multipath conditions ($\alpha=0.9$).

From (3 iii) it is clear that the 'fixed' baseline coordinates do not only rely on the integer ambiguities but also depend on the 'float' baseline coordinates. In case of correctly solved ambiguities the 'fixed' solution can still be biased due to a large bias in the 'float' solution. Therefore we also looked at the number of correctly fixed baseline components in case the ambiguities were fixed correctly. The criterion used for identifying a correct solution of the fixed baseline is an error smaller that 1 centimeter in the horizontal components and smaller than 2 centimeter in the vertical component. The benchmark values for the baseline length and height difference between the two receivers are obtained with a Sokkia Set1X total station. These measurements give us reference values for the observed baseline with a precision of 1 millimeter. Table 5 gives the ratio between the number of epochs with correct baseline solutions and the number of epochs with correctly fixed ambiguities.

The table shows that if the ambiguities are resolved correctly in case of phase-only processing it is likely that the fixed baseline components are also correct. The fixed baseline coordinates in case of code and phase dual-epoch processing are heavily influenced by the multipath errors on the code observations and are generally wrong. This shows that fixing the correct ambiguities does not necessarily give the correct solution for the other unknowns.
4. CONCLUSIONS

In this contribution we studied the epoch-by-epoch or single-epoch RTK-capability of the short-baseline GNSS phase-only model, both in the absence and the presence of multipath. The performance of short-baseline, phase-only integer ambiguity resolution was shown for varying measurement precision, varying observation intervals and for single-, dual- and triple-frequency data varying the number of tracked satellites. Although single-epoch, phase-only ambiguity resolution is impossible, it becomes possible in the dual- and triple-frequency cases when six, respectively, five satellites are tracked.

It was also shown that the phase-only RTK model is more robust against multipath than the standard phase+code RTK model. In particular for attenuations up to $\alpha=0.5$, the phase-only success-rates are significantly larger than those of phase+code. Furthermore it was shown that in case of correct ambiguity resolution, the phase-only fixed baselines are more reliable than their phase+code counterparts.

ACKNOWLEDGMENTS

Professor P.J.G. Teunissen is the recipient of an Australian Research Council Federation Fellowship (project number FF0883188): this support is greatly acknowledged.

REFERENCES


CONTACT

Ir. Lennard Huisman
Spatial Sciences – GNSS Research Lab
Curtin University
GPO Box U1987, Perth, Western Australia, 6845
Tel. +61 (8) 9266 3517
Email: L.Huisman@curtin.edu.au